

# Heterogeneous Initial Stress For Spontaneous Rupture Models: The 2011 Tohoku and 2008 Wenchuan Earthquakes

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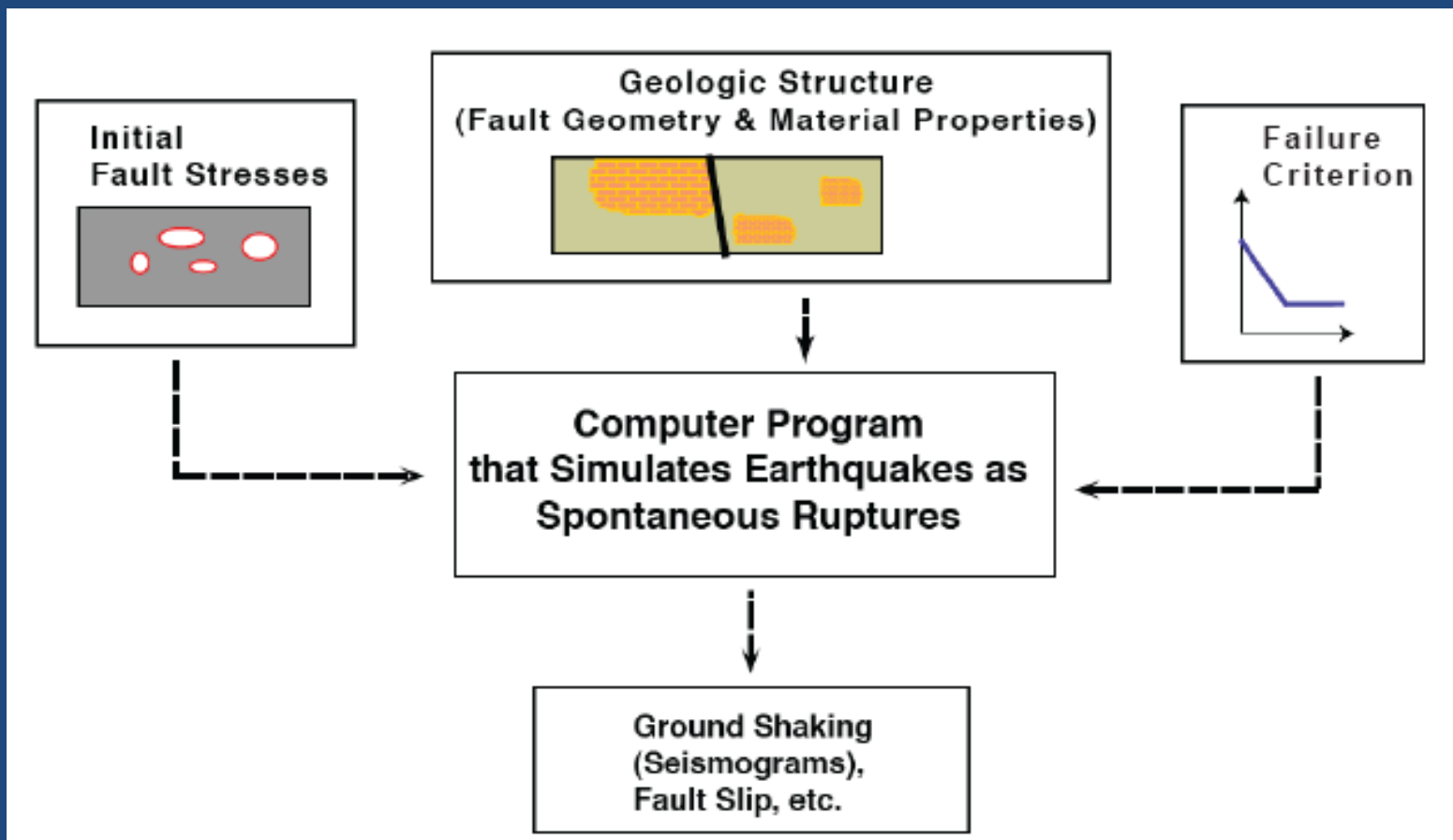
# Outline

- Overview on initial stress setup for dynamic models
- EQdyna: Slip-weakening friction in an elastic or elastoplastic model
- The 2011 M9 Tohoku earthquake: roles of a possible seamount?
- The 2008 M8 Wenchuan earthquake: stress rotations?
- Concluding remarks

# Overview on Initial Stress Setup

# Ingredients of Spontaneous Rupture Models

- Given lab constraints on friction law and geological/geophysical constraints on geologic structure, **Initial stress is the least-constrained ingredient: most important & most flexible?**



# Practice in Specifying Initial Stress

- Constant, depth-independent stress drop: elastic, strike-slip & dip-slip faulting
- Uniform regional stress field: elastic/plastic, strike-slip faulting, e.g., Rice's group work,...
- Depth-dependent initial stress: elastic/plastic, strike-slip & dip-slip faulting, e.g., Andrews et al. (2007), Ma and Andrews (2010),...
- Heterogeneous initial stress: e.g., Day (1982), Andrews & Barall (2011), ...

# Heterogeneous Initial Stress

- Andrews and Barall (2011): random & self-similar (power-law) stress drop, long-wavelength stress variation, GM prediction
- Earthquake-cycle simulation: heterogeneous stress evolves over multi-cycles
  - Lapusta group's work
  - Duan & Oglesby (2005, 2006, 2007)
- Depth-dependent, nonuniform initial stress:
  - Subducted seamounts in 2011 Tohoku EQ?
  - Stress rotations in 2008 Wenchuan EQ?

EQdyna

Brief Overview

# An Explicit FEM Method

- For rupture dynamics and seismic wave propagation
  - One of the codes in the SCEC validation exercise
  - Benefit a lot from our code validation exercise: Thanks to Ruth and All

$$\rho u_{i,tt} = \sigma_{ij,j} + f_i$$

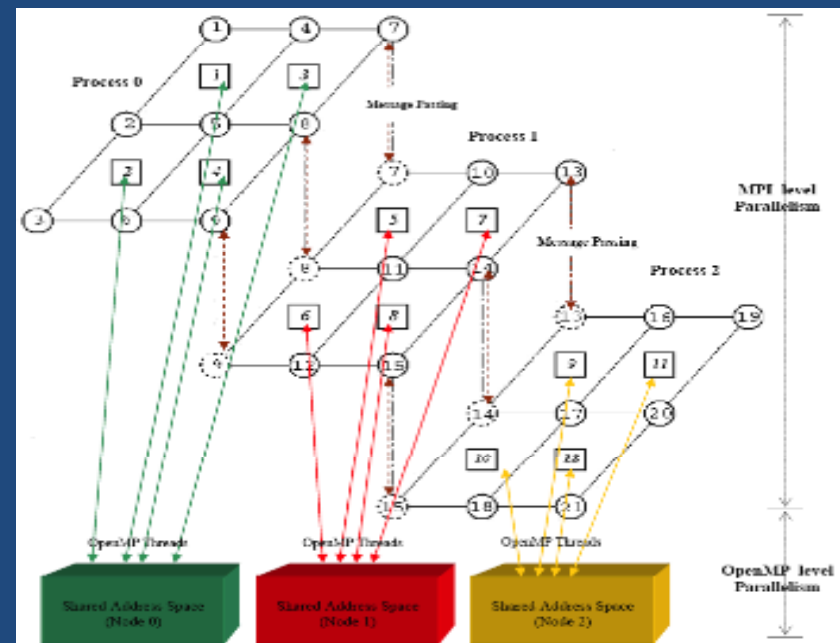
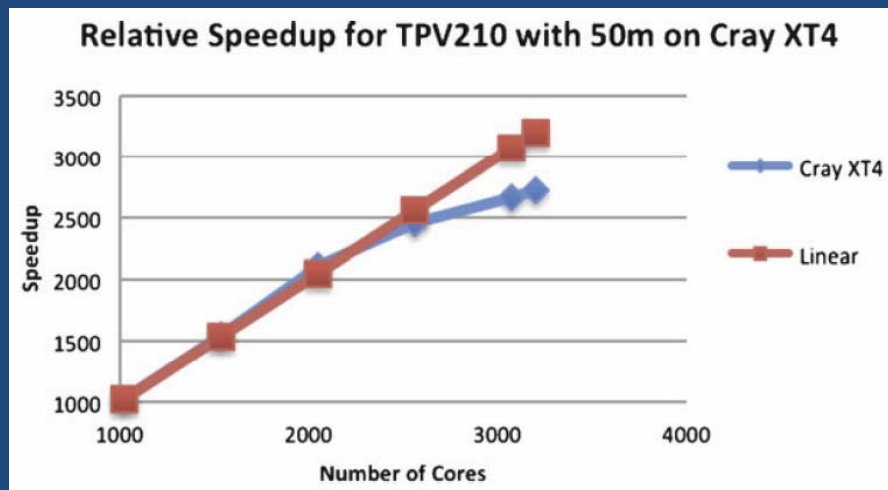
- Slip-weakening friction mainly:
  - rate-state friction in process
- TSN of Day et al. (2005)

$$\tilde{T}_v = \frac{\Delta t^{-1} M^+ M^- [(i_v^+ - i_v^-) + \Delta t^{-1} (u_v^+ - u_v^-) \delta_{vm}] + M^- R_v^+ - M^+ R_v^-}{a(M^+ + M^-)} + T_v^0, \quad v = s, d, n, \quad (4)$$



# Hybrid MPI/OpenMP Parallelization

- For spontaneous rupture modeling of recent large earthquakes: large fault dimension at reasonable element sizes
- Ground motion prediction with dynamic source characterization: high frequency
- Run on large cluster systems: EOS at TAMU, Lonestar & Kraken via NSF



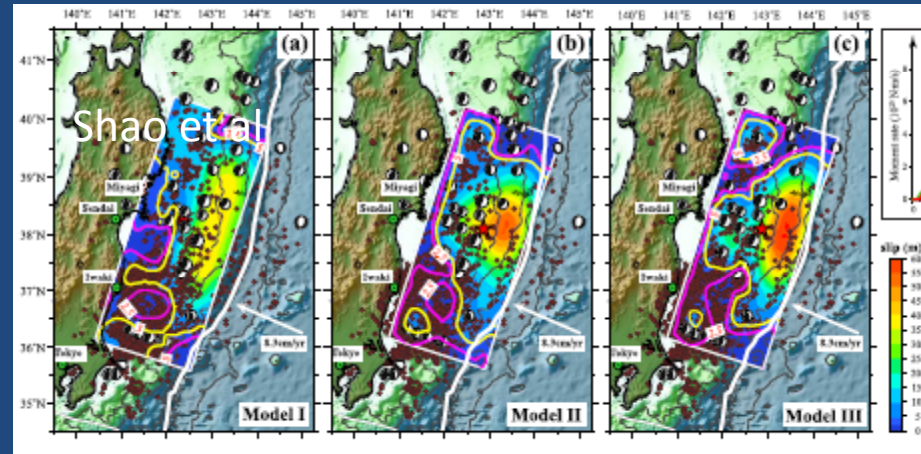
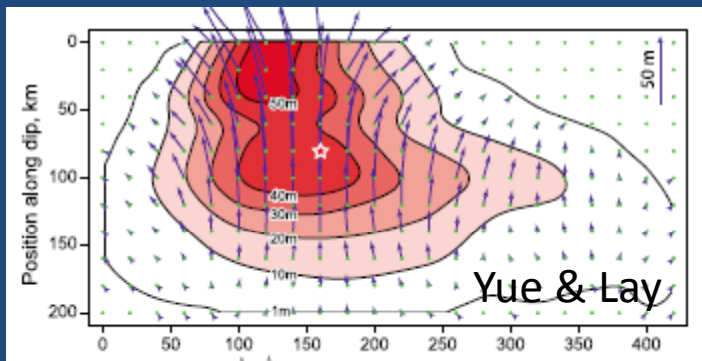
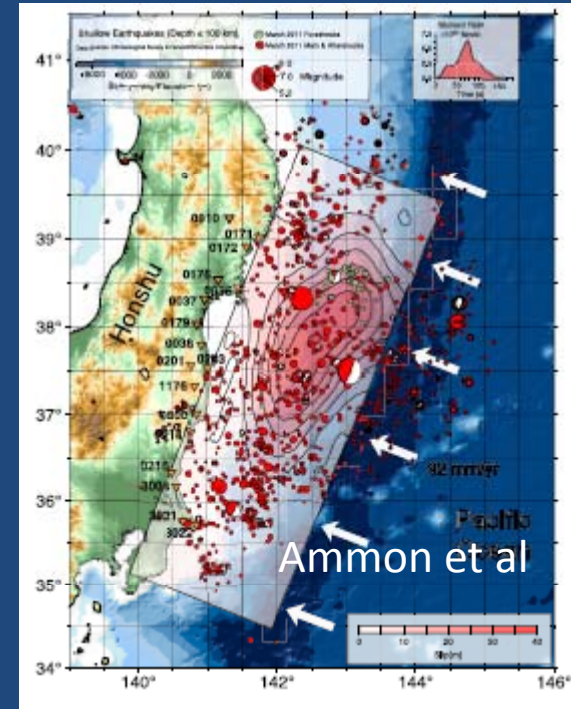
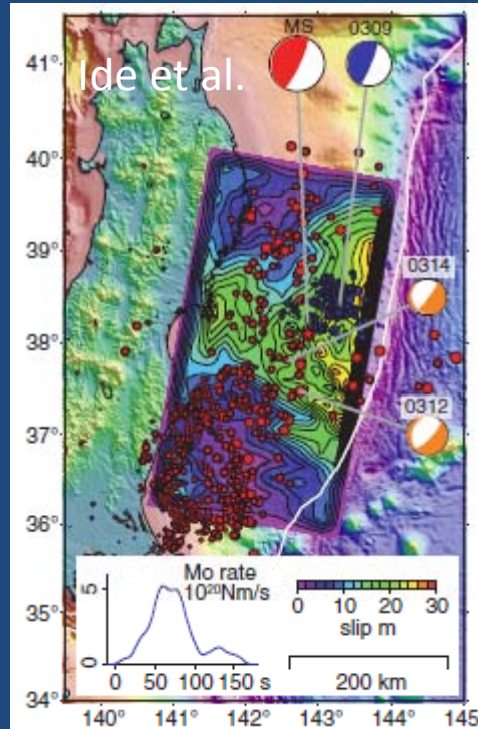
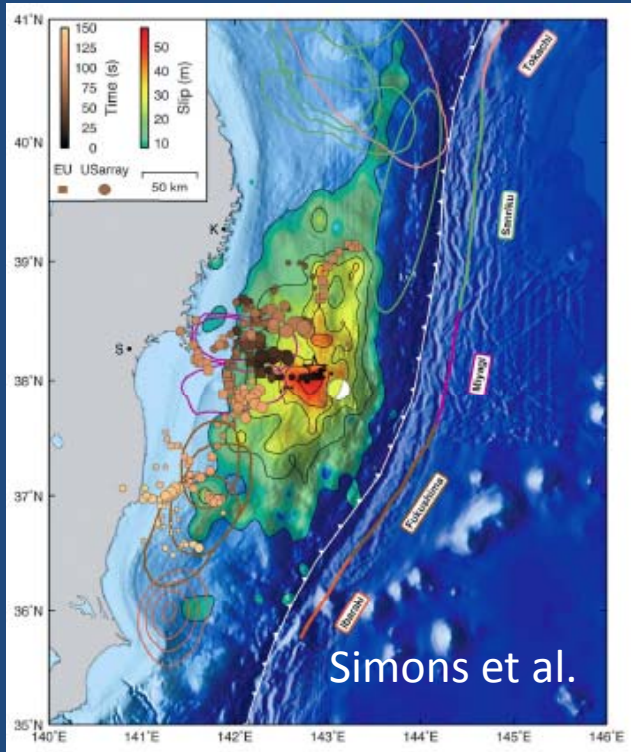
# A Simulation Example

- Parallel computing: a Hybrid MPI/OpenMP approach on multicore supercomputers
  - 500 m element size on  $\sim 440\text{km} \times 220\text{km}$  fault
  - 200 seconds dynamic simulation
  - $\sim 580$  million elements
  - $\sim 35$  hr wallclock time,  $\sim 640$  GB memory using 256 cores for production runs on EOS at TAMU

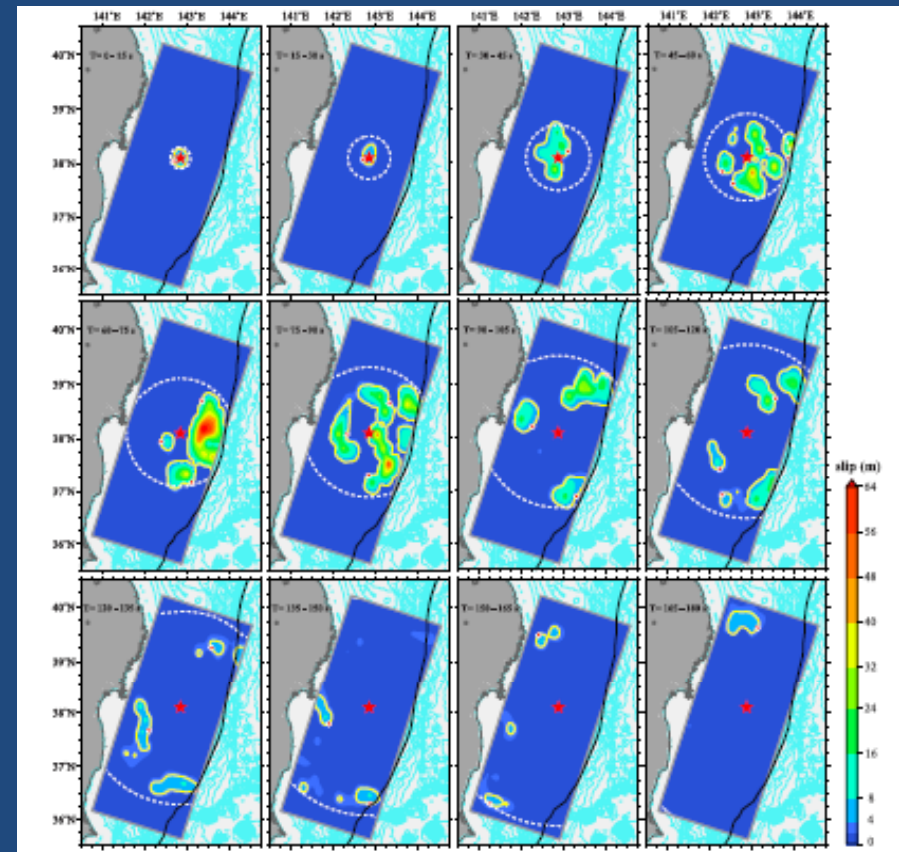
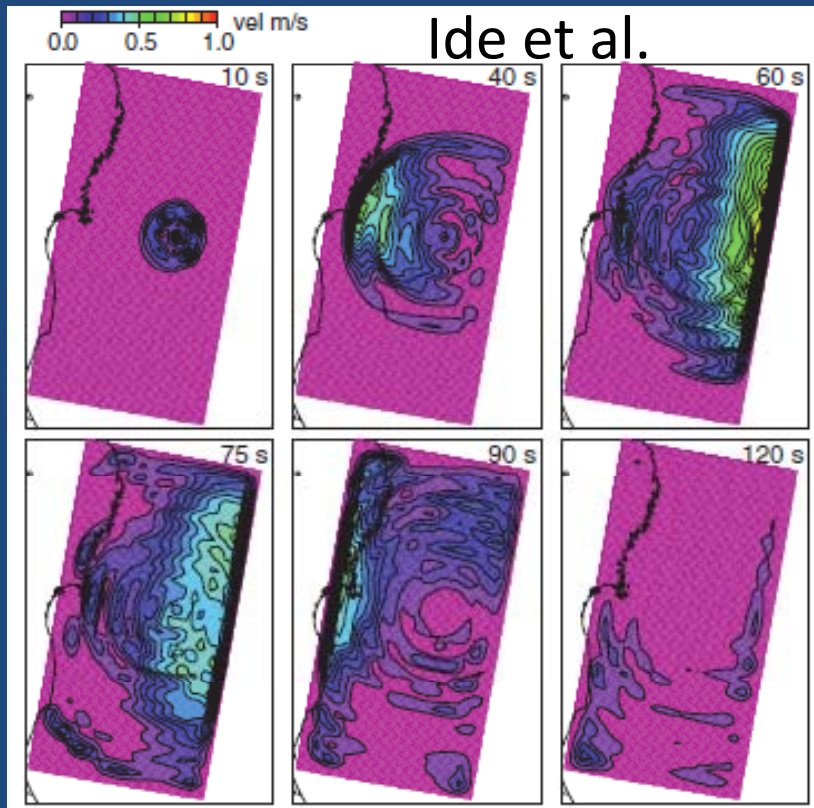
# The 2011 M9 Tohoku EQ

Roles of a Possible Seamount?

# Some Kinematic Inversion Results: Slip



# Some Kinematic Results: Rupture



Shao et al

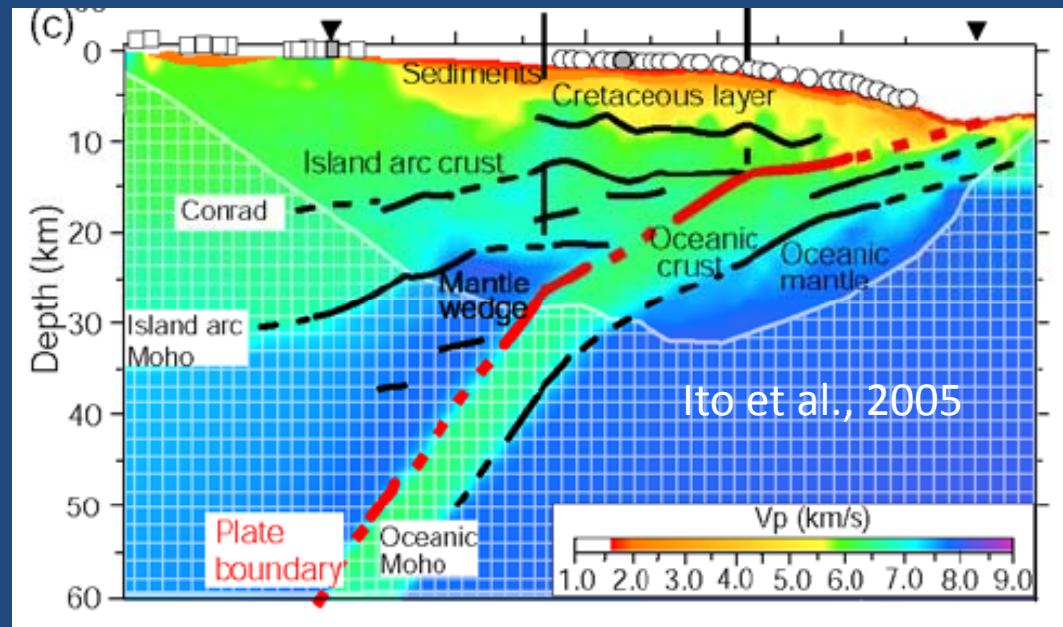
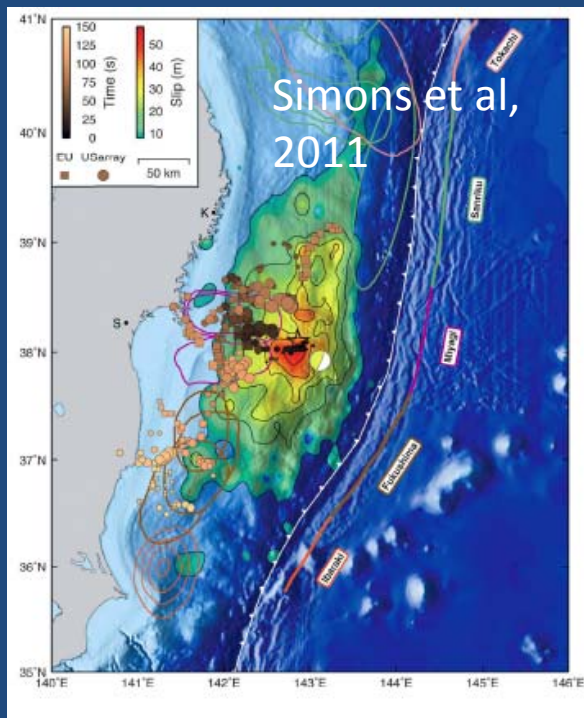
**No up-dip rupture before ~40-45 seconds!**

# Features & Questions

- Large Shallow Slip: 2 competing views
  - max near hypocenter: v-strengthening & stable sliding near trench?
  - max near trench: v-weakening & strain accumulation?
- Rupture propagation
  - No up-dip rupture before ~40-45 seconds: why?
  - Seafloor rupture ~60-75 seconds: strain release (+ stress drop) or passive slip (- stress drop)?
  - Deeper rupture ~90 seconds: what drives?

# What Can Stall Up-Dip Rupture

- Low shear stress vs. **High frictional strength**
- Non-Planar fault geometry vs. **Subducted seafloor features (e.g., Seamounts)**



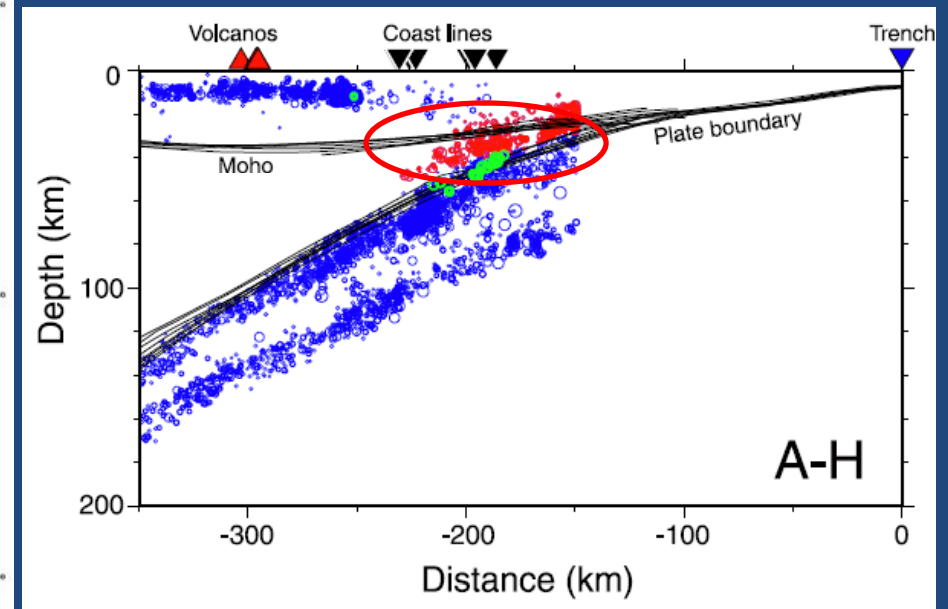
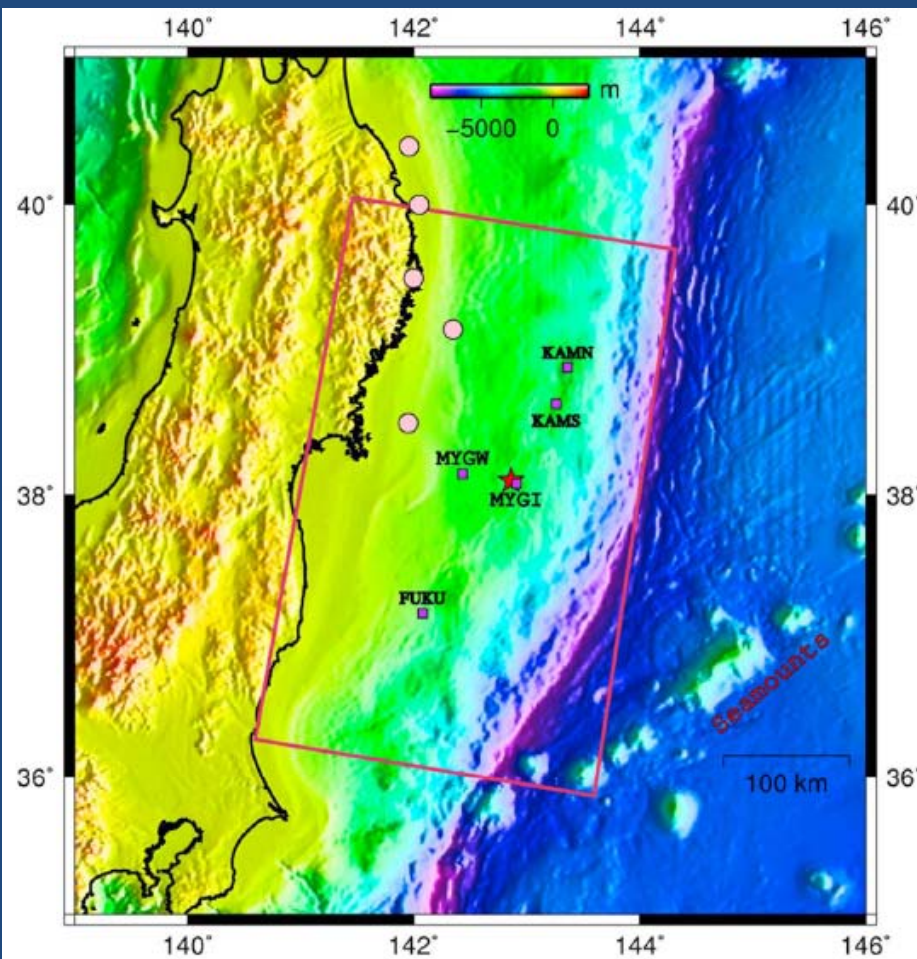
# Subducted Seamounts?

## Bathymetry: ETOPO 1

- Amante & Eakins (2009)

## EQ clusters above the plate face

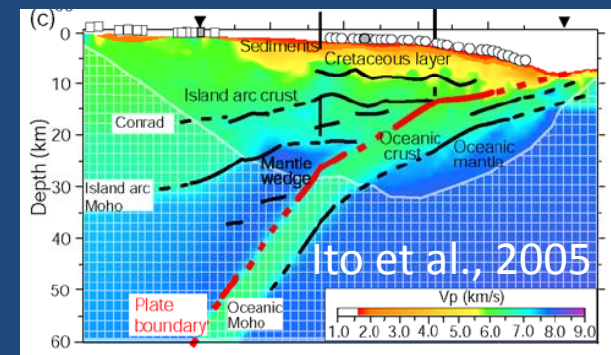
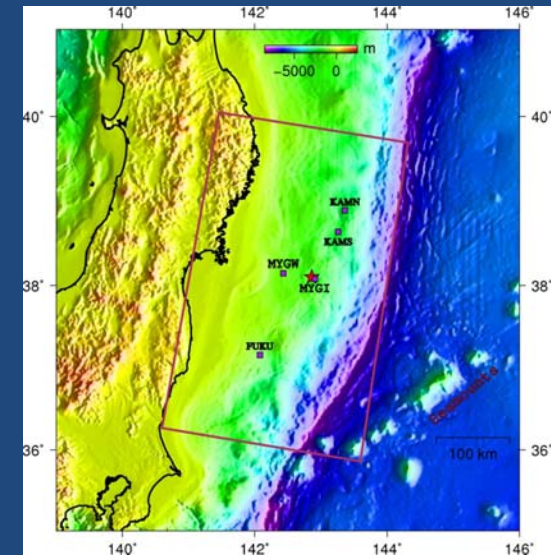
- Uchida et al (2010)





# 3D Spontaneous Rupture Models

- Geology Structure:
  - Fault: a 10° dipping thrust fault
  - Velocity structure: 1D
- Friction Law on Fault: **Slip-weakening**, +/- stress drops mimic V-weakening/strengthening
- Initial Stress: **depth-dependent** normal stress, pore pressure; nominal  $\mu_0$  for initial shear.



# A Procedure of Specifying Initial Stress

- Pure thrust faulting: max and min principal effective stresses are relevant.

$$\sigma_3 = (1 - \lambda)g \int_0^z \rho(z') dz',$$

$$\sigma_1 = R\sigma_3,$$

$$R = [\sin(2\beta) + \mu_0(1 + \cos(2\beta))]/[\sin(2\beta) - \mu_0(1 - \cos(2\beta))].$$

$$\sigma_n = \sigma_1 \sin^2\beta + \sigma_3 \cos^2\beta,$$

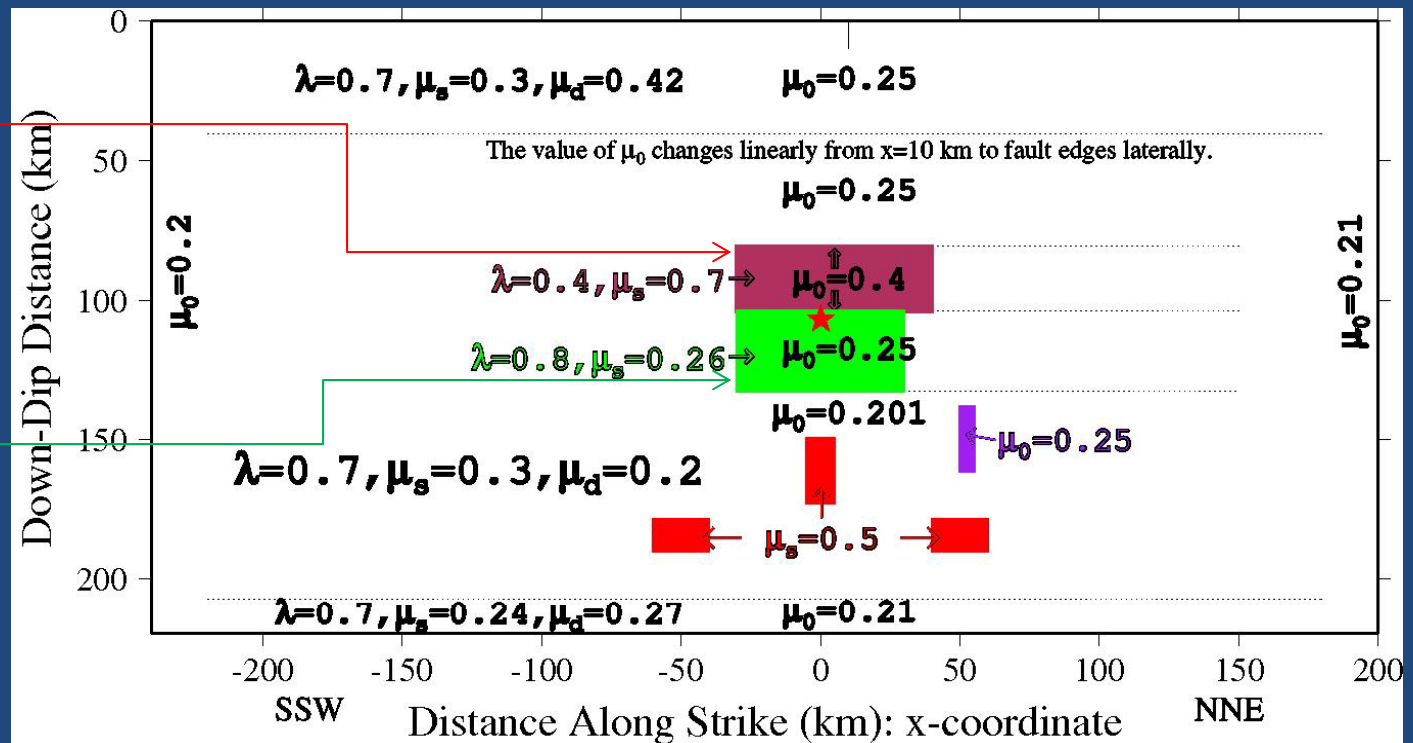
$$\tau_0 = (\sigma_1 - \sigma_3) \sin\beta \cos\beta.$$

# Physical Parameters on the Fault: a Preferred Dynamic Rupture Model

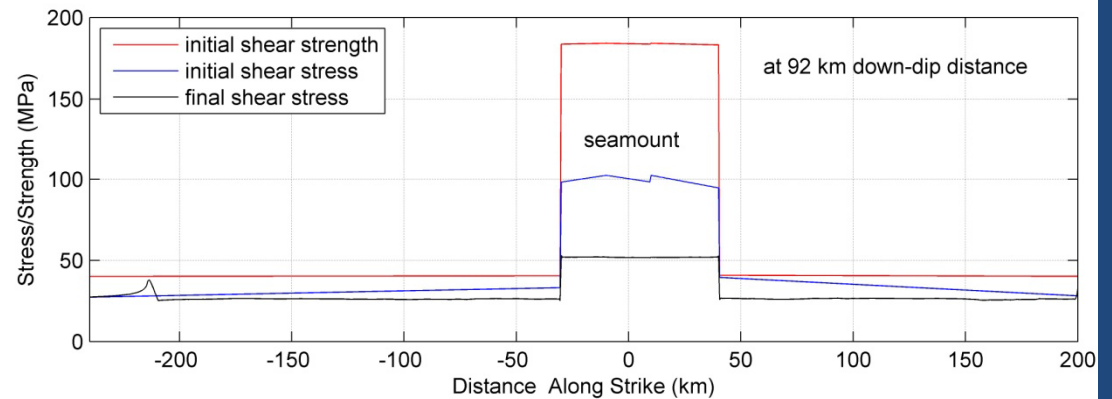
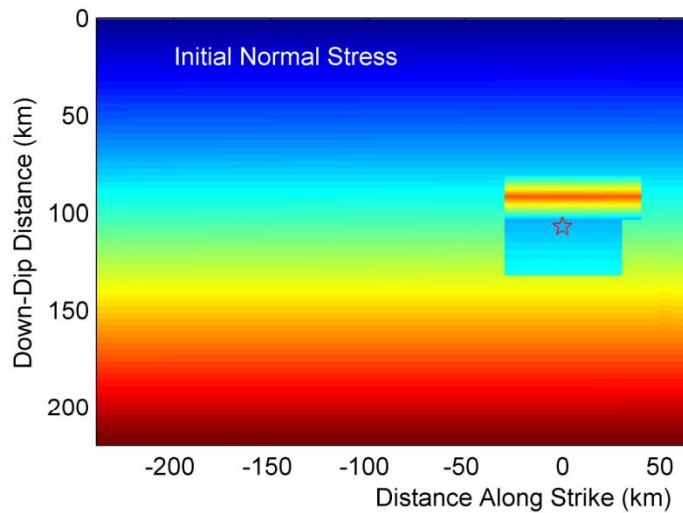
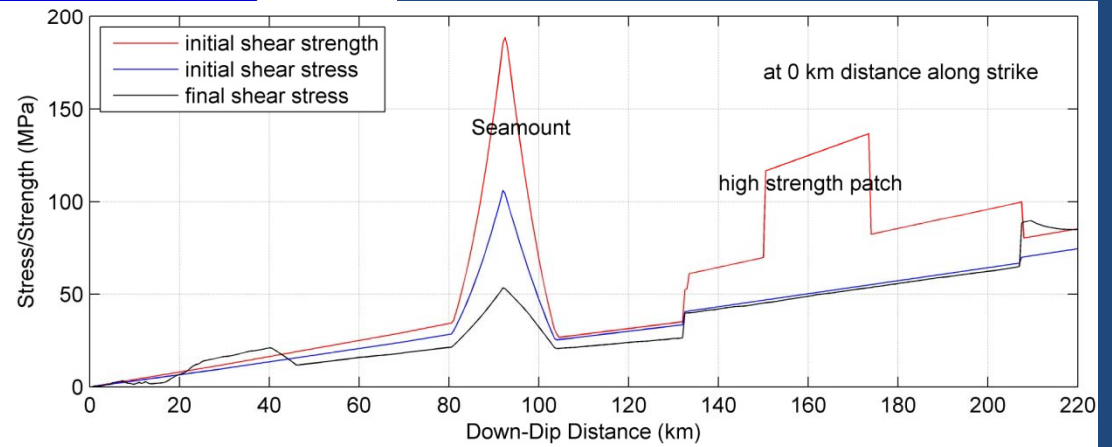
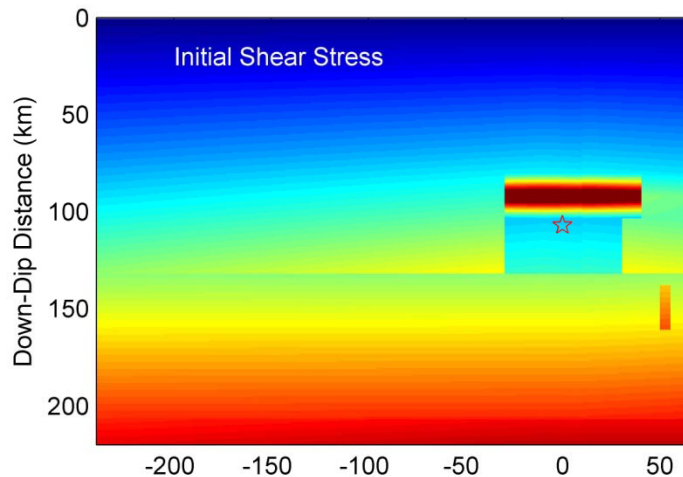
- Pore pressure:  $\lambda$ =pore pressure/lithostatic
- Friction coefficients: static  $\mu_s$  /dynamic  $\mu_d$
- Nominal friction for initial shear stress:  $\mu_0$

Seamount: low  $\lambda$ ,  
high  $\mu_0$ , high  $\mu_s$

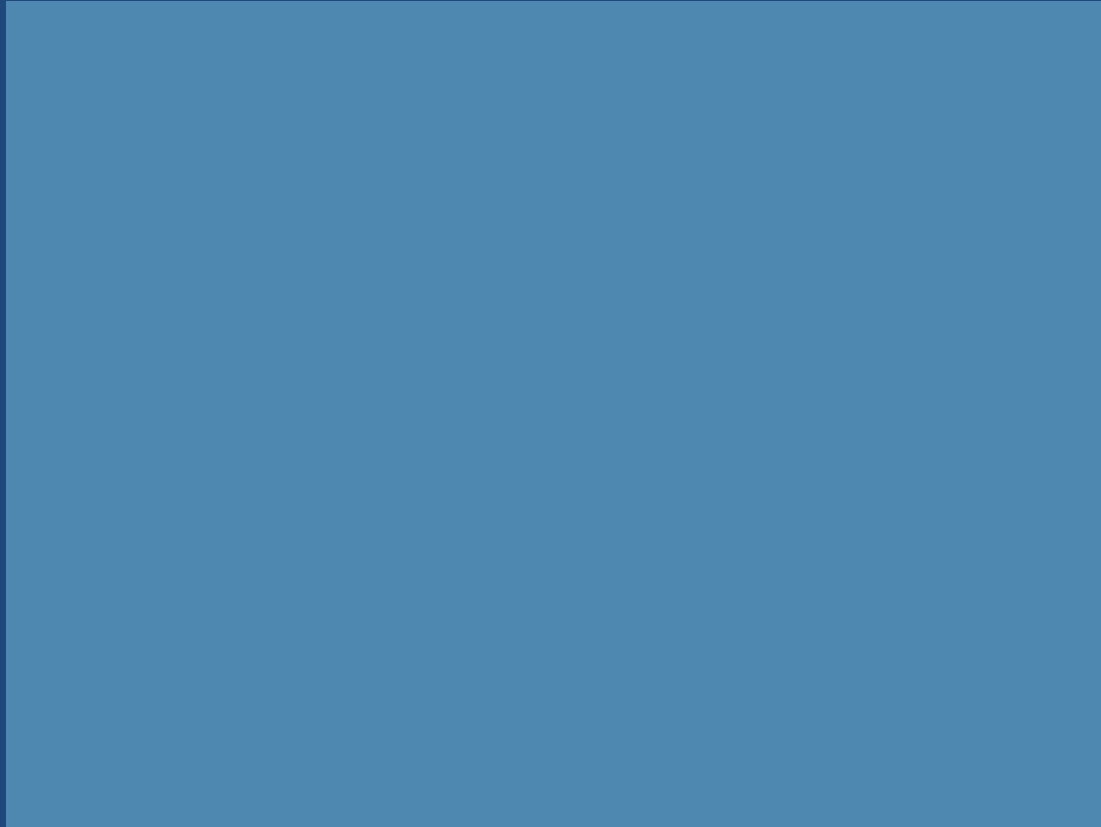
Hypocenter zone:  
high  $\lambda$ , usual  $\mu_0$ ,  
low  $\mu_s$



# Initial Stresses on the Fault

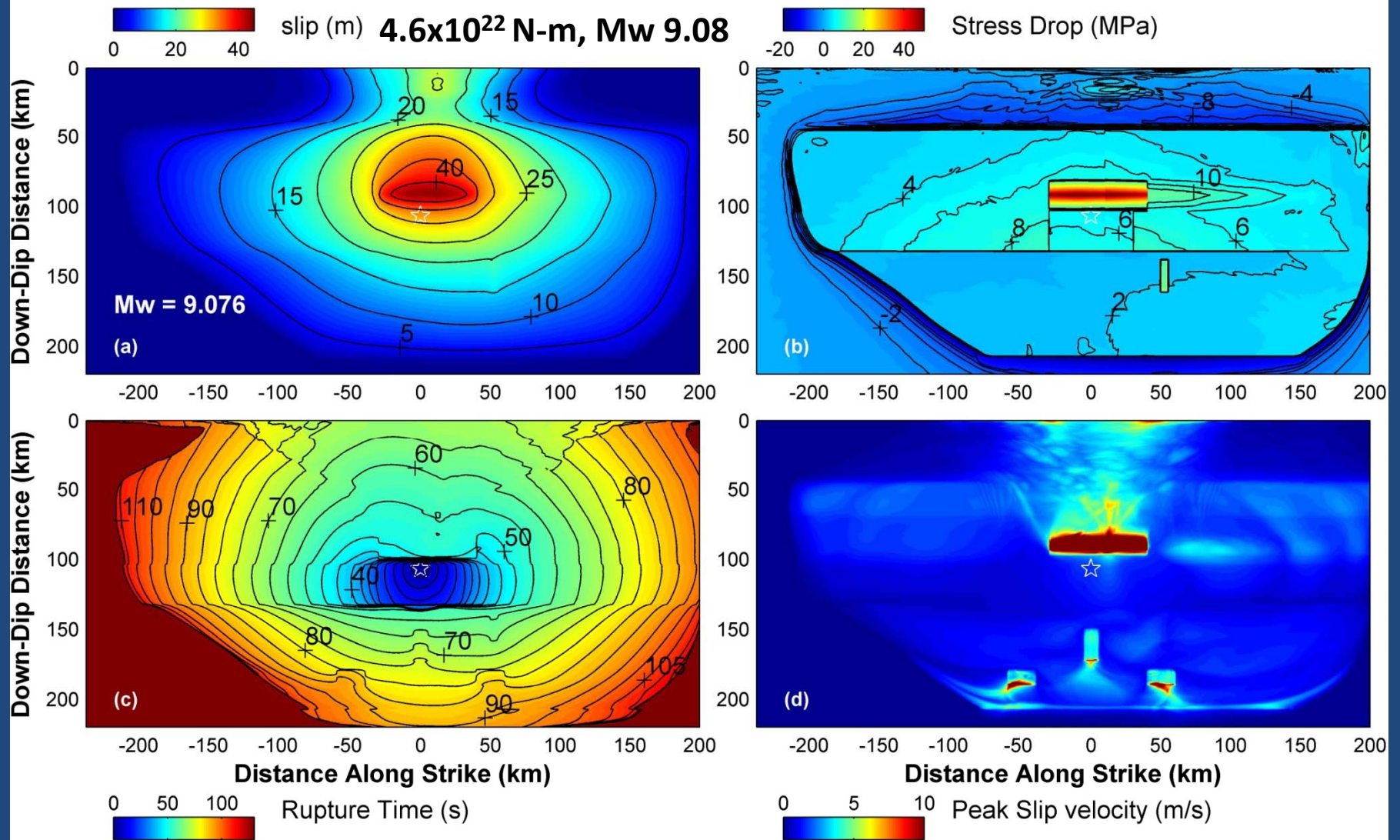


# Dynamic Rupture Propagation



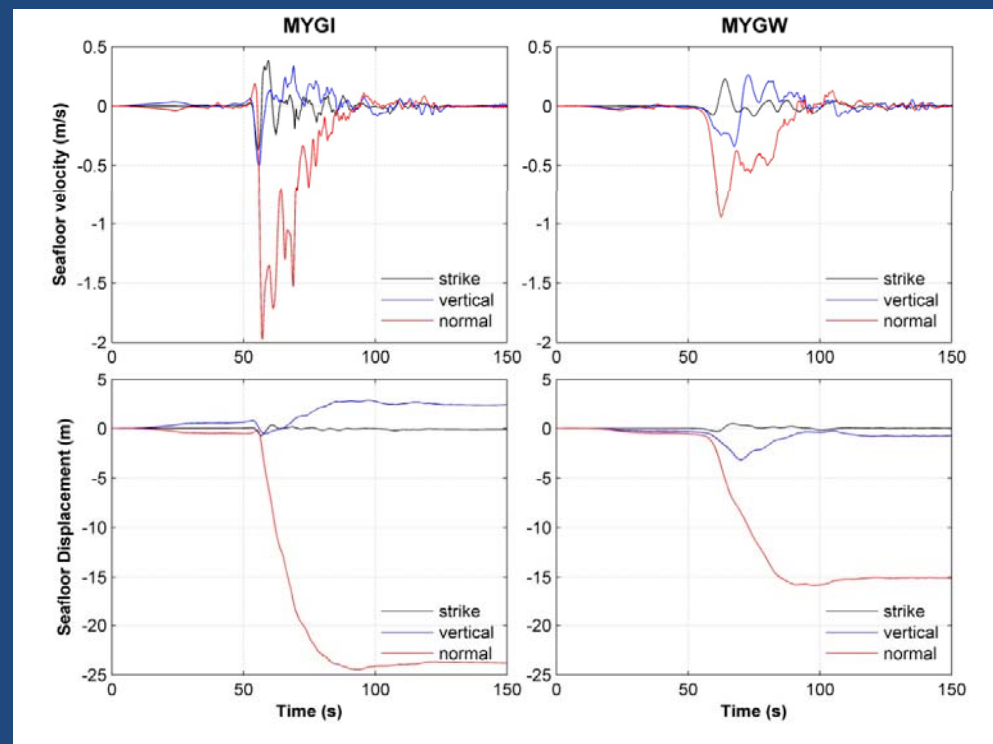
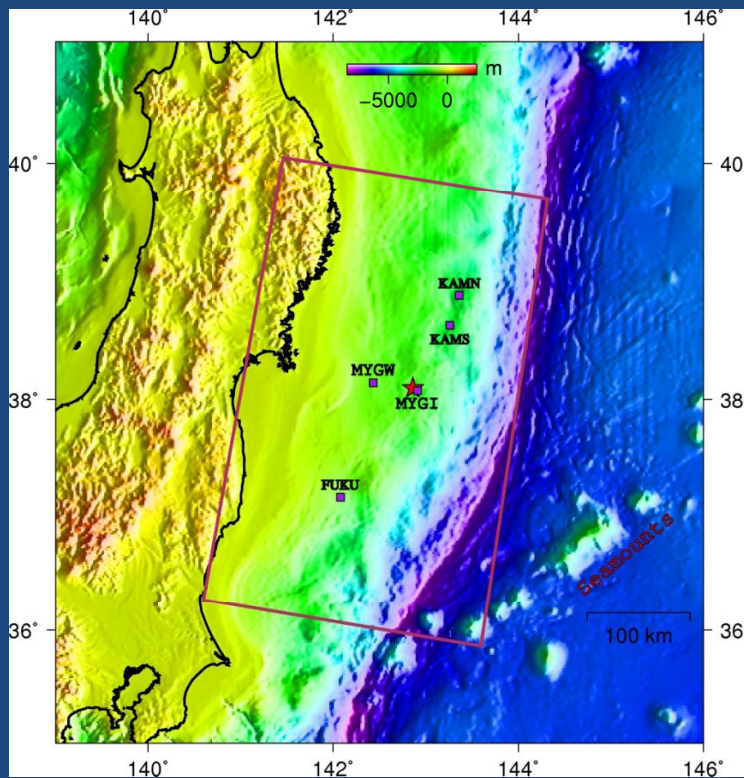
A movie of slip velocity and accumulated slip from the preferred model: see [preferMod.wmv](#)

# Quantities on Fault From the Model



# Reproduce Epicenter Seafloor Displacements

Station	Horizontal Displacement (m)		Vertical Displacement (m)	
	Observed	Simulated	Observed	Simulated
MYGI	24	23.8	3	2.5
MYGW	15	15.0	-0.8	-0.7
KAMS	23	20.0	1.5	5.2
KAMN	15	15.1	1.6	4.3
FUKU	5	5.5	0.9	-1.3

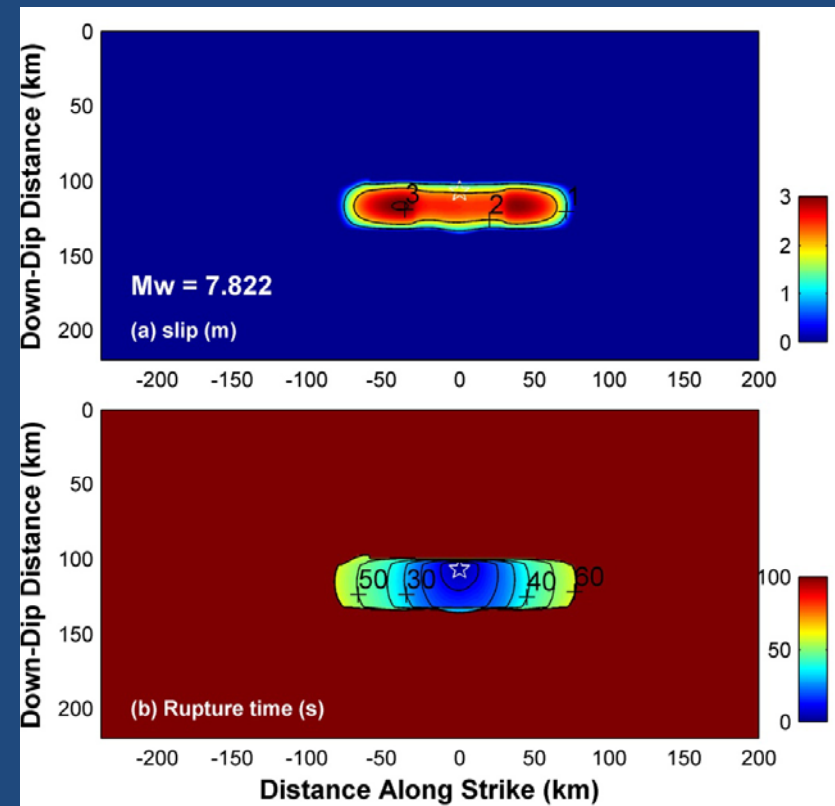


# Importance of the Seamount

- Without other changes, just a longer/stronger seamount: much smaller event



A movie of slip velocity and accumulated slip: see refMod.wmv





# Conclusions on the Tohoku EQ

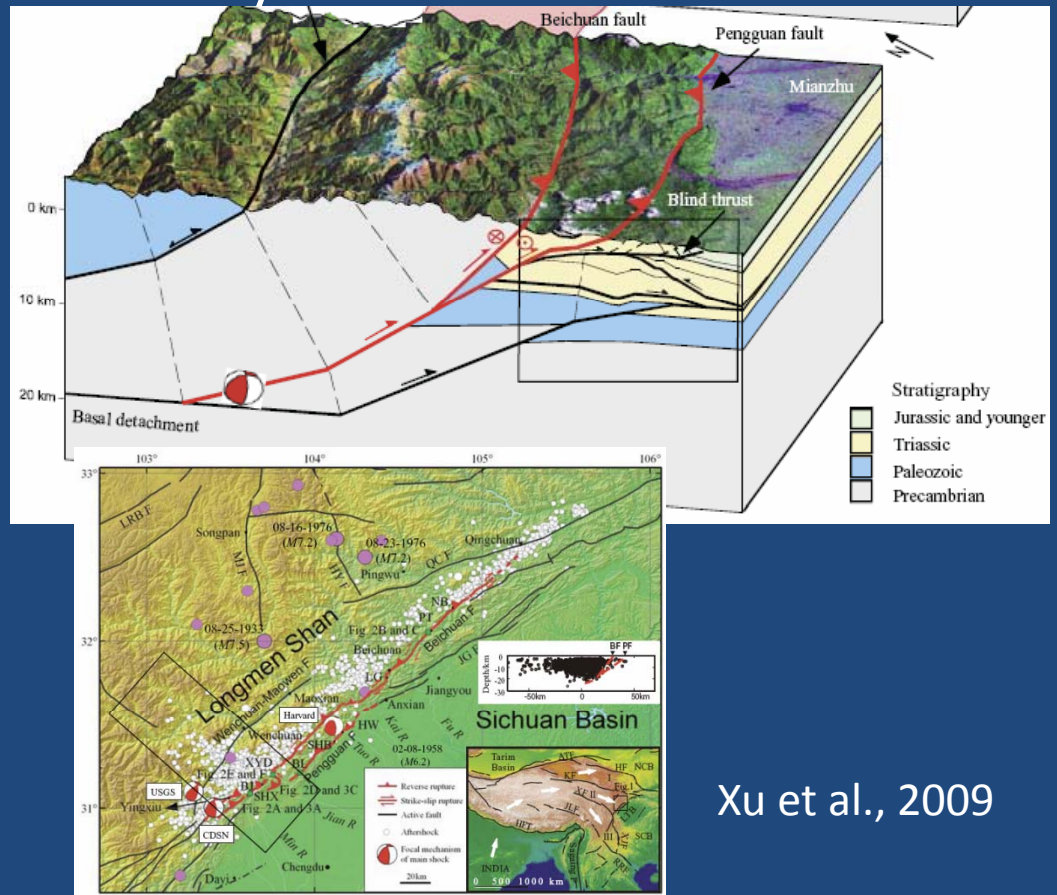
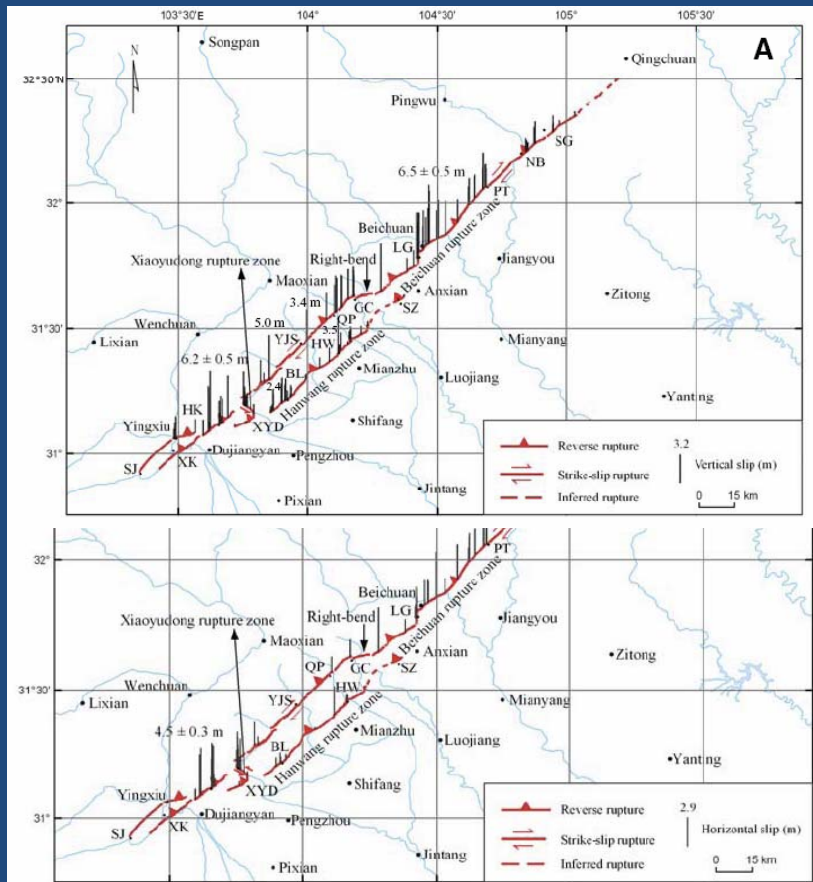
- The 2011 Mw 9.0 Tohoku-Oki earthquake may be primarily controlled by failure of a **~70 km long by 25 km wide subducted seamount**.
  - Located just up-dip of the hypocenter
  - Stalled up-dip rupture: a barrier at beginning
  - Produced max slip  $\sim 50$  m w/ max stress drop of  $\sim 50$  MPa finally: an asperity
- **Large slip near trench may be confined to a small area just up-dip of the seamount**
  - Velocity-weakening (strain accumulation) near trench is not required
  - How strong velocity-strengthening (how large negative stress drop) affects the amplitude of slip there
- **Parallel computing** facilitates exploration of physics of megathrust earthquakes: more dynamic models needed.

# The 2008 Wenchuan EQ

Stress Rotations?

# Field Observations: Surface Rupture

- Two faults ruptured: ~12 km apart on surface
  - Incomplete slip partitioning: oblique on Beichuan fault, thrust on Pengguan fault. Why?
  - Dynamic branching: how and why?



Xu et al., 2009

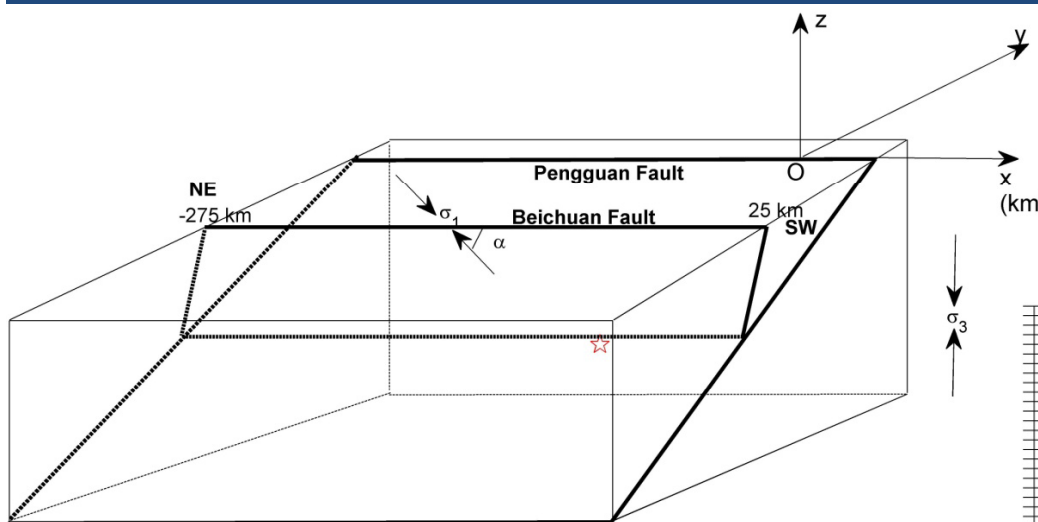
# Kinematic Inversions of Seismic & Geodetic Data

- Complex spatial-temporal evolution of rupture
  - First 16 seconds on Pengguan only
  - Triggered rupture on Beichuan at  $\sim 20$  s and  $\sim 40$  km away

Shao et al., 2010, 2011, 2012

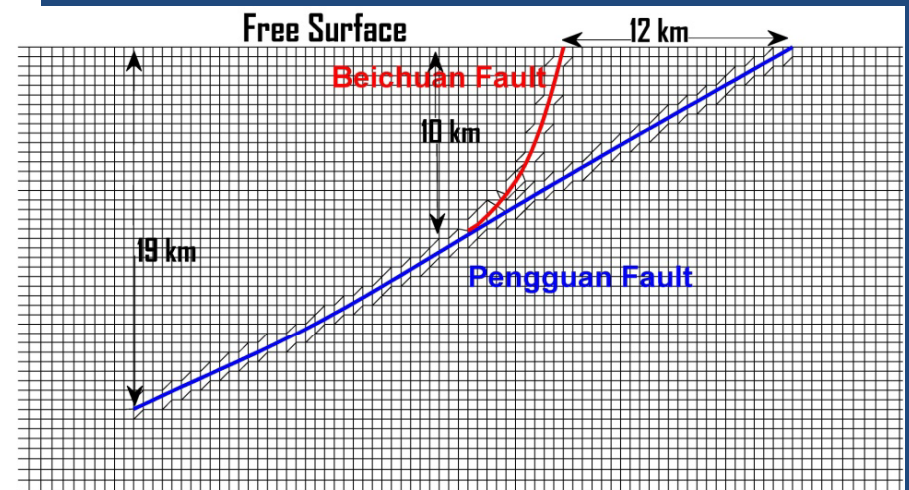
# Our Branched Fault Model

- Two smoothly curved faults: 12 km apart surface, merge at 10 km depth
- Material properties: homogeneous half-space w/ typical crustal rocks
- Friction law: time-weakening (essentially slip-weakening w/ varying  $D_0$ )
- Initial stress: depth-dependent effective stress
  - stress orientations by  $\alpha$  : the angle between  $\sigma_1$  and fault strike (focus of this study)



Setup of initial stresses in the models: as simple as possible

- (1)  $\sigma_3$  is vertical: lithostatic less pore pressure.
- (2)  $\sigma_1$  and  $\sigma_2$  are horizontal.
- (3)  $\sigma_2 = \sigma_3$ .
- (4)  $\sigma_1 = R\sigma_3$ ,  $R > 1$ .
- (5)  $\sigma_1$  makes an angle of  $\alpha$  with the fault strike.



# Uniform Regional Stress Fields

- Cannot produce incomplete slip partitioning
- Cannot produce dynamic branching

# Different $\alpha$ for Two Faults

- Dynamic branching occurs with incomplete slip partitioning.
- But, the triggering feature reported by kinematic inversions is not produced

# Preferred Model: Stress Rotations

- Incomplete slip partitioning
- Dynamic branching by triggering as reported in inversions



# Conclusions on the Wenchuan EQ

- Uniform regional stress orientation along the fault system cannot produce incomplete slip partitioning and dynamic branching features observed in the event.
- Stress rotations between the two faults and along strike of the faults are needed to produce the two features.
  - Evidence: shear-wave splitting

# Concluding Remarks

Heterogeneous Initial Stress for  
Dynamic Rupture Models

# Initial Stress & Dynamic Models

- With observations of recent large earthquakes, dynamic models may allow us to infer initial stress conditions.
- Procedures for specifying initial (principal) stresses that account for depth-dependence & heterogeneities are needed in the dynamic rupture community.